Particle pressure, inertial force and ring current density profiles
in the magnetosphere of Saturn, based on Cassini measurements.

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Abstract

We report initial results on the particle pressure distribution and its contribution to ring current density in the equatorial magnetosphere of Saturn, as measured by the Magnetospheric Imaging Instrument (MIMI) and the Cassini Plasma Spectrometer (CAPS) onboard the Cassini spacecraft. Data were obtained from September 2005 to May 2006, within ±0.5 Rs from the nominal magnetic equator in the range 6 to 15 Rs. The analysis of particle and magnetic field measurements, the latter provided by the Cassini magnetometer (MAG), allows the calculation of average radial profiles for various pressure components in Saturn’s magnetosphere. The radial gradient of the total particle pressure is compared to the inertial body force to determine their relative contribution to the Saturnian ring current, and an average radial profile of the azimuthal current intensity is deduced. The results show that: (1) Thermal pressure dominates from 6 to 9 Rs, while thermal and suprathermal pressures are comparable outside 9 Rs with the latter becoming larger outside 12 Rs. (2) The plasma β (particle/magnetic pressure) remains ≥1 outside 8 Rs, maximizing (~3 to ~10) between 11 and 14 Rs. (3) The inertial body force and the pressure gradient are similar at 9-10 Rs, but the gradient becomes larger ≥11 Rs. (4) The azimuthal ring current intensity develops a maximum between approximately 8 and 12 Rs, reaching values of 100-150 pA/m². Outside this region, it drops with radial distance faster than the 1/r rate assumed by typical disk current models even though the total current is not much different to the model results.
Introduction

The Saturnian ring current was initially inferred from magnetic field [Connerney et al., 1981 and 1983] and particle [Krimigis et al., 1981 and 1983; Mauk et al., 1985] measurements during the Voyager 1 and 2 flybys, and studied in more detail with Cassini [Krimigis et al., 2007; Sergis et al., 2007 and 2009; Arridge et al., 2007 and 2008; Brandt et al., 2008; Kellett et al., 2009].

The planetary ring current is located between ~8 and ~18 Rs (Rs=60268 km), in a region where plasma is slowed with respect to corotation [Wilson et al., 2008; McAndrews et al., 2009], primarily composed of O\(^+\) ions and characterized by increased suprathermal (>3 keV) particle pressure with high (>1) plasma β and intense dynamic behavior. The physical mechanisms, however, governing the characteristics and dynamics of the ring current are not fully understood. Bunce et al. (2007) studied the ring current using magnetic field measurements and an axisymmetric model [Connerney et al., 1983], arguing that the ring current is dominated by inertial currents. Sergis et al. (2009) showed that the average radial suprathermal pressure gradient is sufficient to modify the radial force balance and the azimuthal current.

Since July 1 2004, Cassini is orbiting Saturn and monitors its magnetospheric environment via in-situ and remote measurements. In this study we combine particle data with magnetic field measurements for radial distances between 6 and 15 Rs. Energetic particles are sampled by the Charge Energy Mass Spectrometer (CHEMS) sensor of the Magnetospheric Imaging Instrument (MIMI) [Krimigis et al., 2004]. Sergis et al. (2009) have shown that the observed intensities are generally representative of the energetic
particle intensity perpendicular to the local magnetic field. The magnetic field vector is
measured by Cassini’s fluxgate magnetometer [Dougerty et al., 2004].

Plasma properties are measured with the ion mass spectrometer (IMS) and the electron
spectrometer (ELS), parts of the Cassini plasma spectrometer (CAPS) [Young et al.,
2004]. The IMS measures ions between 1 eV/e and 50 keV/e while the ELS has a
measurement range of 0.6 eV/e to 28 keV/e. Both sensors are mounted on an actuating
platform providing directional flux measurements.

Since the field-of-view (FOV) pointing of the CAPS sensors depends on the
orientation of the spacecraft, it is not always possible to measure plasma quantities such
as pitch angle distributions or flow velocity, thus limiting the calculation of plasma
moments determined by forward modeling techniques [e.g. Lewis et al., 2008] to a subset
of available data. For the present study we have employed plasma moments that were
calculated based on numerical integration of the observed IMS singles (SNG) count rates
for times when the nominal plasma corotation flow direction was in the FOV of the IMS,
and for which no warning flags were set (c.f., Thomsen et al., 2009, in preparation). In
addition, we have included the inner magnetosphere parameter set derived by forward
modeling [Wilson et al., 2008] and those for the tail region [McAndrews et al., 2009].

The CAPS and MIMI ion sensors overlap between 3 and 45 keV. However, the
amount of actual double bookkeeping does not correspond to the full range of this
overlap, mostly due to the different geometrical factors and sensitivity of the two sensors
and the average spectral shape in the regions of interest. Our analysis of typical spectra
suggests that the resulting overestimation of the total plasma pressure is <25% and is well
masked by the natural scatter in the data.
The availability of ion plasma moments and the existing suprathermal pressure profile [Sergis et al., 2009] offer for the first time the opportunity of computing the total particle pressure. In this study we present radial profiles for the pressure components in the equatorial magnetosphere of Saturn, expanding previous works by Sergis et al., (2007 and 2009), and Wilson et al., (2008). The results reveal an azimuthal current with maximum intensity of 100-150 pA/m², primarily due to the plasma pressure gradient. We note that energetic neutral atom (ENA) images obtained by the ion and neutral camera (INCA) of MIMI show that the instantaneous ring current is non-uniform (partial ring current) [e.g. Carbary et al., 2008], indicating that any study utilizing long term measurements can only depict the average state of the middle magnetosphere and likely underestimate peaks in the ring current. Moreover, the fact that most of the magnetospheric parameters (density, pressure, ENA emission, magnetic field) are longitude dependent imposes an a-priori limitation to any symmetric ring current model. A detailed study addressing orbit-to-orbit variability in the ring current including comparison with model predictions for the radial dependence of the current density is currently in preparation by Kellett et al.

Results

The radial profile for different pressure components in the Saturnian magnetosphere is shown in Figure 1a. It is evident that, despite significant scatter in the data, the thermal plasma pressure is dominant for \( r \leq 9 \) Rs, while the suprathermal pressure progressively prevails for \( r \geq 12 \) Rs. The thermal electron pressure remains lower than the ion pressures by a factor of \( \sim 10 \). Schippers et al., (2008) showed that during one pass the suprathermal
electron pressure was significant between 9 and 15 $R_S$, compared to the average shown in Figure 1a. A direct comparison during that pass (not presented here), showed the ion pressure to be higher than the average shown. Thus, neglecting the suprathermal electron pressure is not expected to significantly affect our conclusions. The total particle pressure (panel b) is relatively flat between 6 and 8 $R_S$ with typical values close to 0.4 nPa, but drops by $\times 10$ by 15 $R_S$. The total particle pressure is almost equal to measured magnetic pressure ($\beta \approx 1$) near 8 $R_S$, while beyond 9 $R_S$ the particle pressure dominates with $\beta$ reaching values of 3 to 10 between 11 and 14 $R_S$. A high $\beta$ regime in this region was also reported by Sergis et al. (2009), with lower, however, values, as it did not include the thermal plasma pressure, while Sittler et al. (2008) also reported a thermal plasma pressure close to the magnetic pressure near the distance of Rhea (8.7 $R_S$), based on measurements from the Saturn Orbit Insertion (SOI).

The radial profile of the total particle pressure indicates that its decay region ($r>7 R_S$) is characterized by a significant (negative) gradient. Assuming that the plasma is corotating with constant angular velocity and all ion components have the same bulk velocity, the radial, steady-state form of the force balance equation in the equatorial plane can be written as:

$$\rho \frac{V_\phi^2}{r} - \frac{\partial P}{\partial r} - \frac{P_\perp}{R_C} \left( A - I \right) \approx J_\phi B_z$$

(1) with $\rho$ the plasma mass density, $V_\phi$ the in-situ measured azimuthal flow velocity, $P$ the total particle pressure, $P_\perp$ the field perpendicular thermal pressure component, $R_C$ the curvature of the field lines, $A$ the thermal plasma pressure anisotropy ($A = P_\perp/P_\parallel$, $P_\parallel$ being the parallel thermal pressure), $J_\phi$ the azimuthal current density and $B_z$ the magnetic field.
component normal to the nominal equatorial plane. The 3 terms on the left side represent
the inertial, the pressure gradient and the pressure anisotropy components of the force in
the radial direction. When solving for $J_\phi$, equation (1) becomes:

$$J_\phi \approx \frac{I}{B_i} \left( \frac{V_\phi^2}{r} - \frac{\partial P}{\partial r} - \frac{P_\perp}{R_C} \left( \frac{A-I}{A} \right) \right)$$  \hspace{1cm} (2)

Figure 1c shows the radial profile of the inertial body force $\rho \frac{V_\phi^2}{r}$ (see also Thomsen
et al. in preparation) with an exponential fit to the measured data and dashed lines to
represent a 1-\(\sigma\) zone of the distribution. This profile is shown together with the particle
pressure gradient ($-\frac{\partial P}{\partial r}$) and the anisotropy force $F_A = -\frac{P_\perp}{R_C} \left( \frac{A-I}{A} \right)$ in Figure 1d,
illustrating their relative contribution to the ring current vs. radial distance. The
anisotropy force was directly calculated (and consecutively fitted) from the thermal
pressure anisotropy measurements available for 6 to 10 $R_S$ [Wilson et al., 2008]. Analysis
of long term magnetic field measurements shows that for these radial distances the dipole
approximation can be safely used to determine the magnetic curvature as $R_C=\theta/3$. The
pressure radial gradient comes from differentiating the polynomial fit (Figure 1b) to the
total particle pressure. Inside ~9 $R_S$ (neutral cloud) the anisotropy force is significant, but
remains lower by a factor of 2 to 3 compared to the inertial body force which prevails due
to the higher mass density and plasma angular velocity in that region. Between 9 and 10
$R_S$ the inertial and pressure gradient terms are comparable, while further out the latter
becomes greater by a factor of 2 to 5, indicating that in this part of the magnetosphere,
the ring current is primarily pressure gradient-driven and modified by the energetic
particle population, especially during injection events [Mauk et al., 2005; Paranicas et al.,
2007], when the suprathermal pressure is significantly increased and the local mass density is lower.

Having all components of equation (2) either directly measured or derived from the data permits the calculation of the corresponding ring current density. In Figure 2a the inertial, the pressure gradient and the pressure anisotropy components of $J_{\phi}$ are shown. Inertial and pressure gradient currents are similar between 9 and 10 $R_S$; beyond that range the inertial ring current drops quickly. The increased scatter for $r>10$ $R_S$ is primarily due to fluctuations in the suprathermal pressure.

The total ring current density profile is presented in Figure 2b together with an $r^{-2.2}$ function that describes quite well the decrease of the measured ring current density for $r>11$ $R_S$. The red dashed line (dotted for $r>10$ $R_S$) shows the total current density when the anisotropy current is included. The estimates of the inertial ring current from the model of Connerney et al. (1983, Voyager measurements) and Bunce et al., (2007, Cassini measurements) are also shown. The measured ring current density develops a maximum region between 8 and 12 $R_S$, not predicted by either model, but in agreement with Mauk et al., (1985) and Beard et al., (1987, Figure 3 therein), reaching values of 100-150 pA/m$^2$. As evident from Figure 2a, this maximum $J_{\phi}$ region is imposed by the pressure gradient.

It is interesting to examine under what conditions (i.e. relative magnitudes of $\rho \frac{V^2}{r}$ and $-\frac{\partial P}{\partial r}$) a maximum in $J_{\phi}$ develops. Figure 3 is a parametric study of the radial profile of the total $J_{\phi}$ for different (lower) values of particle pressure gradient, while the inertial term is kept constant. The maximum in the ring current starts forming for pressure
gradient even 4 times smaller than that measured, indicating that the ring current is strongly affected by the particle pressure even during times of moderate magnetospheric activity.

Summary and discussion

The key questions that this study addresses are: (1) What is the radial profile of each pressure component in the equatorial magnetosphere of Saturn? How do different pressures compare for different radial distances? (2) Can we determine if the azimuthal ring current $J_\phi$ is inertial, pressure gradient-driven or a combination of both? What is its radial dependence?

Plasma, energetic particle and magnetic field measurements by Cassini used to calculate the total particle pressure and its radial gradient for a large part of the equatorial magnetosphere show that: (1) Typical values of the particle pressure are 0.4 nPa (6 $R_S$) dropping to 0.05 nPa (15 $R_S$), with plasma $\beta > 1$ outside 8 $R_S$ and maximum values of ~3 to 10 between 11 and 14 $R_S$. (2) The contribution of the energetic particles to the total particle pressure becomes significant at >9 $R_S$ and progressively overtakes the thermal plasma beyond 12 $R_S$. (3) The inertial body force and the radial pressure gradient (and consequently their contribution to $J_\phi$) are comparable at 9-10 $R_S$ with the pressure gradient becoming greater outside of 11 $R_S$, while the inertial force prevails inside 8.5 $R_S$. (4) Inclusion of the anisotropy current (dashed/dotted curves in Figure 2b) affects the total current mostly in the inner part (~60% maximum decrease at 6 $R_S$) compared to the maximum region (~10 % at 10 $R_S$). The shape of the $J_\phi$ profile does not change noticeably. (5) The ring current density develops a maximum between 8 and 12 $R_S$
reaching values of 100-150 pA/m², in the same region where maximum ENA emission has been observed [Carbary et al., 2008] and suprathermal electron pressure increases, with electron $\beta \sim 1$ [Schippers et al., 2008]. Outside this region, $J_\psi$ drops with radial distance much faster than the $1/r$ dependence that disk current models assume ($J_\psi \propto r^{-2.2}$ outside ~10 Rs). Further analysis indicates that the maximum in $J_\psi$ would be present even for a considerably lower (factor of 3 to 4) pressure gradient (moderate magnetospheric activity), while the $1/r$ decrease does not represent the data well for any relative strength of the terms contributing to $J_\psi$. As the suprathermal electron pressure is not included in our study (not yet available for more than one orbit), the pressure gradient deduced here could be somewhat underestimated.

Our results confirm that Saturn possesses an intense and variable ring current, which is primarily inertial at $<8.5$ Rs but increasingly pressure gradient-driven in its maximum region (8 to 12 Rs) and certainly farther out. This fact needs to be accounted for, when modeling the magnetosphere-ionosphere coupling (mapping the magnetospheric regions into the ionosphere). The predictions of certain disk models (e.g. Connerney et al., 1983, 2004, Bunce et al., 2007) are consistent with the deduced total current, but cannot describe successfully the ring current radial density profile as observed by Cassini.

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Figure captions

Figure 1. (a): Radial pressure profile for thermal ion plasma (blue), energetic particles (red) and thermal electron plasma (black), together with polynomial fits of the same color. The apparent scatter is indicative of the intense dynamics present in the Saturnian magnetosphere. Electron moments are not available inside 10 R_S due to the spacecraft potential noise. (b): Radial profiles for the magnetic pressure (black) and the total particle pressure (blue), with a polynomial fit of the same colors. (c): Radial dependence of the inertial body force. The blue solid line is an exponential fit to the data, while dashed lines bracket a 1-σ zone of the distribution. (d): Radial profiles of the inertial body force (blue), the particle pressure gradient (red) and the pressure anisotropy force (black). The blue line is the exponential fit shown in panel c, the red line is the derivative of the polynomial fit to the total pressure (shown in panel b).

Figure 2. (a): Radial profiles for the inertial \( \left( \frac{I}{B_z} \rho \frac{V_\phi^2}{r} \right) \), the pressure gradient \( \left( -\frac{I}{B_z} \frac{\partial P}{\partial r} \right) \) and the pressure anisotropy \( -\frac{P_z}{B_z R_C} \left( \frac{A-I}{A} \right) \) contribution to the total current density \( J_\phi \) in blue, red and gray (solid for the measured, dotted for the extrapolated part) respectively. The ring current progressively changes from purely inertial inside of 8 R_S, to pressure gradient-driven for \( r \geq 11 \) R_S. (b): Radial profile of the total ring current density \( J_\phi \). The red line is a moving average, the green line is a polynomial fit to the data, while the black line represents an \( r^{-2.2} \) power low. The blue line is the \( J_\phi \) output of the Connerney-1983 model (Voyager data) and the orange lines correspond to the min and max \( J_\phi \) profiles.
produced by Bunce (2007, Cassini data). The red dashed line (dotted for \(r>10 \, R_S\)) is the total current density if the pressure anisotropy current is included.

**Figure 3.** Total ring current density profiles for different contributions of the pressure gradient term (0.1, 0.25, 0.5 and 1.0 of the measured \(-\frac{\partial P}{\partial r}\), in green, blue, red and black respectively). The dash-dotted lines show the same results if the anisotropy current is included.
\[
\log P = a_0 + a_1 r + a_2 r^2 + a_3 r^3 + a_4 r^4
\]

- \( a_0 = -13.13664 \)
- \( a_1 = 1.51845 \)
- \( a_2 = -0.21660 \)
- \( a_3 = 0.01264 \)
- \( a_4 = -2.73574 \times 10^{-4} \)

\[
F_c = (1.33E-16) \times \exp[-r/1.91] - 1.46E-20
\]

\[
\log(-F_{AN}) = -23.1768 + 2.6749 \times r - 0.3866 \times r^2 + 0.01647 \times r^3
\]

- \( a_0 = -4.39455 \times 10^{-17} \)
- \( a_1 = 1.58329 \times 10^{-17} \)
- \( a_2 = -2.03087 \times 10^{-18} \)
- \( a_3 = 1.12519 \times 10^{-19} \)
- \( a_4 = -2.29316 \times 10^{-21} \)
(a) \[ J_{\phi} \text{ (pA/m}^2 \text{)} \]

(b) \[ J_{\phi} \text{ (pA/m}^2 \text{)} \]

Pressure grad current
Inertial current
Anisotropy current

\[ J_{\phi} \text{ polynomial fit} \]
\[ J_{\phi} \text{ moving average} \]

\[ r^{-2.2} \]

Figure 2
The graph shows the variation of the current density $J_{\phi}$ (pA/m^2) as a function of range ($R_S$) for different multiples of the derivative $dP/dr$. The legend indicates the following lines:

- Black solid line: $1.00 \times dP/dr$
- Red solid line: $0.50 \times dP/dr$
- Blue solid line: $0.25 \times dP/dr$
- Green solid line: $0.10 \times dP/dr$

The variations are depicted with 6 distinct curves, each representing a different multiple of the derivative, and range from 0 to 200 on the $y$-axis.